

THE SEEBECK COEFFICIENT OF GRAPHITE  
OR  
THE STB MODEL REVISITED

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For the purpose of investigating the thermoelectric power of graphite we consider it a fair approximation to describe the majority-carrier bands by means of

$$E_{e,h} = E_0(\xi) \pm \hbar^2 \kappa^2 / 2m^*(\xi), \quad (1)$$

where  $E_0(\xi) = 2\gamma_2 \cos^2(\xi/2)$  and  $m^*(\xi) = (4/3)(\hbar/a_0)^2 (\gamma_1/\gamma_0^2) \cos(\xi/2)$ . In terms of this model, and using standard notations, the free carrier concentration amounts to

$$n_e + n_h = \frac{\langle m^* \rangle}{2\pi \hbar^2 c_0} \int_{-\pi}^{+\pi} \cos(\xi/2) d\xi \int_{-\infty}^{+\infty} |E - E_0(\xi)| \left(-\frac{\partial f_0}{\partial E}\right) dE, \quad (2)$$

which is found to be almost independent of  $\gamma_2$  for  $kT \gg \gamma_2$ . Since we are concerned with temperatures in the range above 300°K, we conclude that for all practical purposes we may set  $E_0(\xi) \equiv 0$ , or in other words, ignore the effects of "overlap" in the frame of this work.

With  $a = n_h/n_e$  and  $b = \mu_e/\mu_h$ , the Seebeck coefficient of graphite (layer-plane configuration) is best expressed as follows:

$$\alpha_{||} = (a\alpha_h + b\alpha_e)/(a+b), \quad (3)$$

where  $\alpha_e = -\frac{k}{e} \left( \frac{K_1}{kTK_0} - \frac{E_F}{kT} \right)$  and  $K_1 = \frac{1}{4\pi^3} \int_{BZ} \tau_e v_x^2 E^1 \left(-\frac{\partial f_0}{\partial E}\right) d^3k$  --- similar

expressions hold for the hole contribution  $\alpha_h$ . Following McClure [Proc. Fifth Carbon Conf. 2, 3(1963) 1], we assume that the relaxation times may be derived from the "golden rule" for transition probabilities and thus that, within the approximation  $\gamma_0 \equiv 0$ , we have energy-independent relaxation times. On this basis it is a straightforward matter to demonstrate that

$$\alpha_{||} = (k/e)(a+b)^{-1} [a(\mathcal{J}_+ - \Delta/kT) - b(\mathcal{J}_- + \Delta/kT)] \quad (4)$$

with  $\mathcal{J}_{\pm} = [2\mathcal{F}_1(\pm \Delta/kT)] [\mathcal{F}_0(\pm \Delta/kT)]^{-1}$ , where  $\mathcal{F}_j$  designates a Fermi-Dirac integral and  $\Delta$  measures the Fermi-level depression ( $\Delta = -E_F$ ).\*

We will show that data obtained in the range 0° to 1000°C for various classes of pyrolytic graphite (PG) substantiate Eq.(4) and lead to the following conclusions: (a) In graphitized PG the mobility ratio  $b$  increases slowly with temperature and may reach 1.2 at 800°C (see attached figure); (b) In turbostratic PG the Seebeck coefficient behaves in accordance with a Fermi level depressed by  $\approx 0.015$  eV and changes sign above 1000°C; (c) In boronated PG the temperature dependence of  $\alpha_{||}$  differs drastically with boron content though metallic characteristics emerge at B/C  $\geq 0.3$  %.

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This accords with a previous result of Klein [J. Appl. Phys. 35, 2947 (1964) 1], but does no longer involve unrealistic assumptions such as spherical energy surfaces and acoustic lattice scattering.

