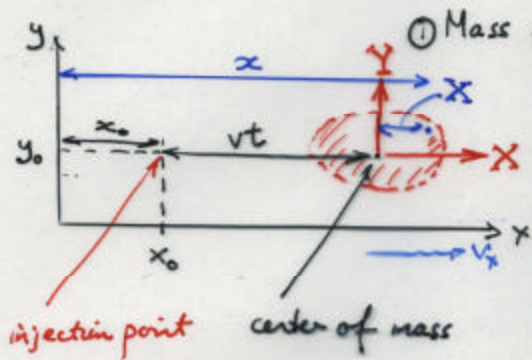


### 5.6.6 3-D Flow field - Slug Injection

$$C(x, y, z, t) = \frac{M}{8(\pi t)^{3/2} \sqrt{D_x D_y D_z}} \exp \left\{ -\frac{(x - (x_0 + vt))^2}{4D_x t} - \frac{(y - y_0)^2}{4D_y t} - \frac{(z - z_0)^2}{4D_z t} \right\}$$

(M = C<sub>0</sub> × volume)



- ① Mass of injection at location  $x_0, y_0, z_0$
- ② Moves downstream @ velocity  $v$
- ③ At time,  $t$ , center of mass at  $x = x_0 + vt$

Note coordinates:  $x_0 + vt + X = x$   
 $X = x - (x_0 + vt)$

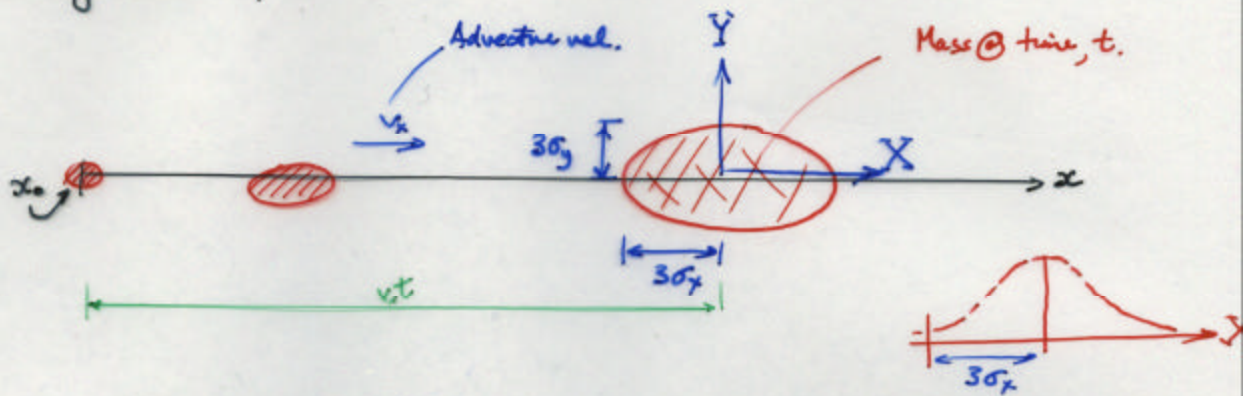
∴ substitute into (1)

$$C = \frac{M}{8(\pi t)^{3/2} \sqrt{D_x D_y D_z}} \exp \left\{ -\frac{X^2}{4D_x t} - \frac{Y^2}{4D_y t} - \frac{Z^2}{4D_z t} \right\}$$

Max concentration; set  $X = Y = Z = 0$

$$C_{max} = \frac{M}{8(\pi t)^{3/2} \sqrt{D_x D_y D_z}}$$

Note down gradient form:



Zone consisting of 99.7% of Mass  
contained in the 3-D ellipsoid of  
dimensions:

$$3\sigma_x = 3\sqrt{2D_x t} = 3(2D_x t)^{1/2} \text{ etc.}$$

$$3\sigma_y = 3\sqrt{2D_y t}$$

$$3\sigma_z = 3\sqrt{2D_z t}$$

- ∴ ① Measure ellipsoid in field  
and ② evaluate  $D_x$  etc.

Preferable method since includes large scale heterogeneity

