


## 5.5 ADVECTION-DISPERSION EQUATION

Summing the diffusive and advective components:


$$n \frac{\partial c}{\partial t} = n \left\{ \frac{\partial}{\partial x} D_x \frac{\partial c}{\partial x} + \frac{\partial}{\partial y} D_y \frac{\partial c}{\partial y} + \frac{\partial}{\partial z} D_z \frac{\partial c}{\partial z} \right\} - \left\{ \frac{\partial}{\partial x} (v_x^d c) + \frac{\partial}{\partial y} (v_y^d c) + \frac{\partial}{\partial z} (v_z^d c) \right\}$$

Reduces to:

1-D case:  $D_L \frac{\partial^2 c}{\partial x^2} - \frac{v_x^d}{n} \frac{\partial c}{\partial x} = \frac{\partial c}{\partial t}$



2-D case:  $D_L \frac{\partial^2 c}{\partial x^2} + D_T \frac{\partial^2 c}{\partial y^2} - \frac{v_x^d}{n} \frac{\partial c}{\partial x} = \frac{\partial c}{\partial t}$



Usual assumptions:

- Homogeneous medium
  - Constant value of  $D_L, D_T$
- } analytical solutions
- Heterogeneous
  - Velocity dependent  $D_L, D_T$
- } numerical solutions.